



Department of Geography and Earth Sciences

**WRM 625**

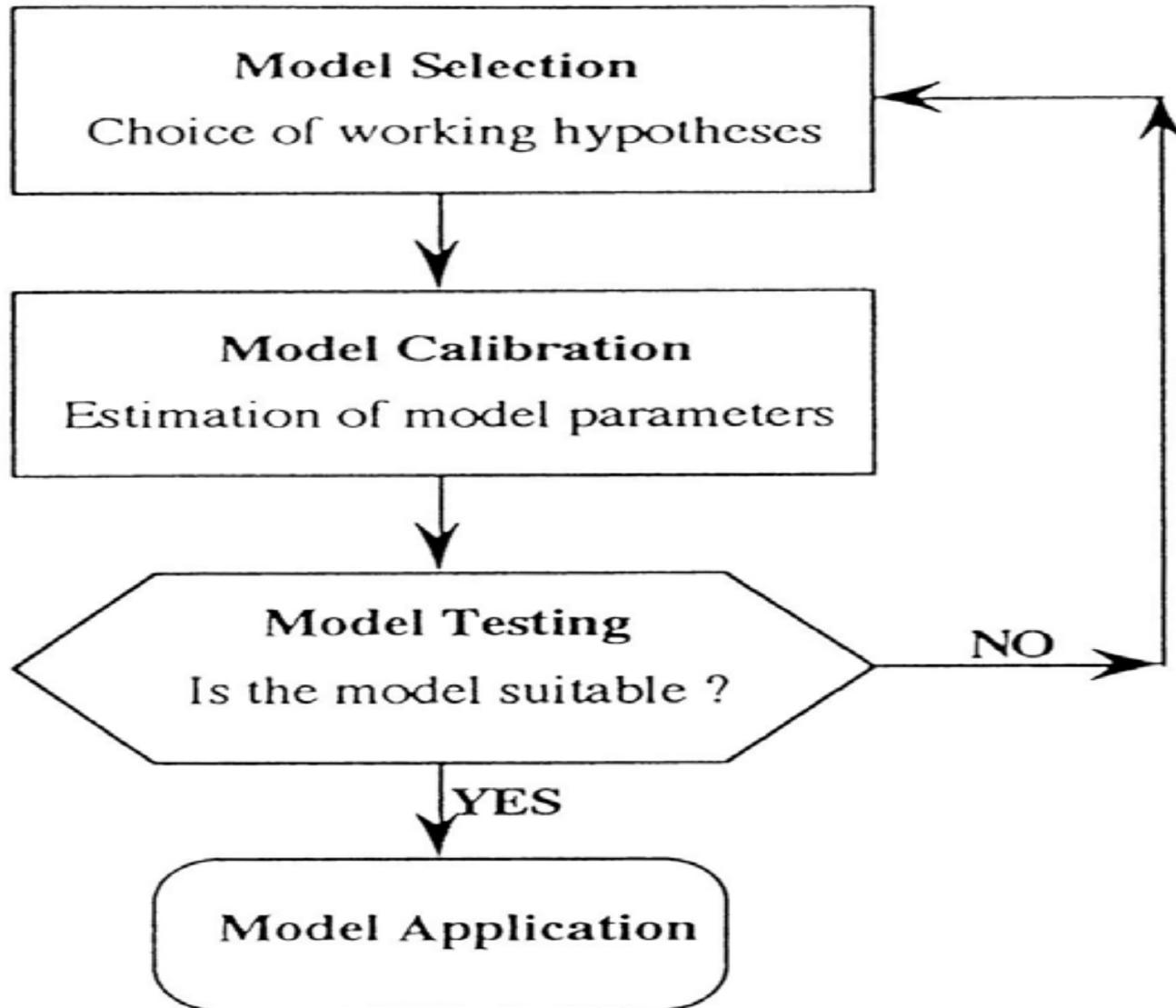
Hydrological Modeling: Calibration, Verification,  
Validation, and Sensitivity Analysis

**Lecture 3**

# PHASES OF MODEL EVALUATION

- Levels of model evaluation
  - (i) model selection – choice of working hypotheses
  - (ii) model calibration - estimation of the parameter values
  - (iii) model validation - testing the fitted model to verify its accuracy; and
  - (iv) estimation of its range of applicability

# Phases of Model Evaluation



# Calibration

- All models have unknown constants used to represent the physical process.
- These constants are called model parameters and must be assigned fixed numerical values before the model may be used to predict the runoff .
- There must be agreement between Observed and simulated flow
- The process by which the parameters are selected is called model “calibration”.

# Model Parameters

**a) Physical parameters:** represent physically measurable properties of the watershed.

- Examples the area of the watershed, the fraction of the watershed area that is impervious, the surface area of the streams and open water bodies, surface slopes.

**(b) Process parameters:** process parameters represent watershed properties that are not directly measurable. Examples : the average or “effective” depth of surface soil moisture storage, the effective lateral interflow rate, the coefficient of nonlinearity controlling rate of percolation to the groundwater storage

# Parameter determination

- **Parameter specification:** prior knowledge about the watershed properties and behaviour to specify initial estimates for the parameters of the model
  - Physical parameters: from field measurements and fixed
  - Process parameters: estimates of the range determined based on knowledge of the watershed and adjusted.

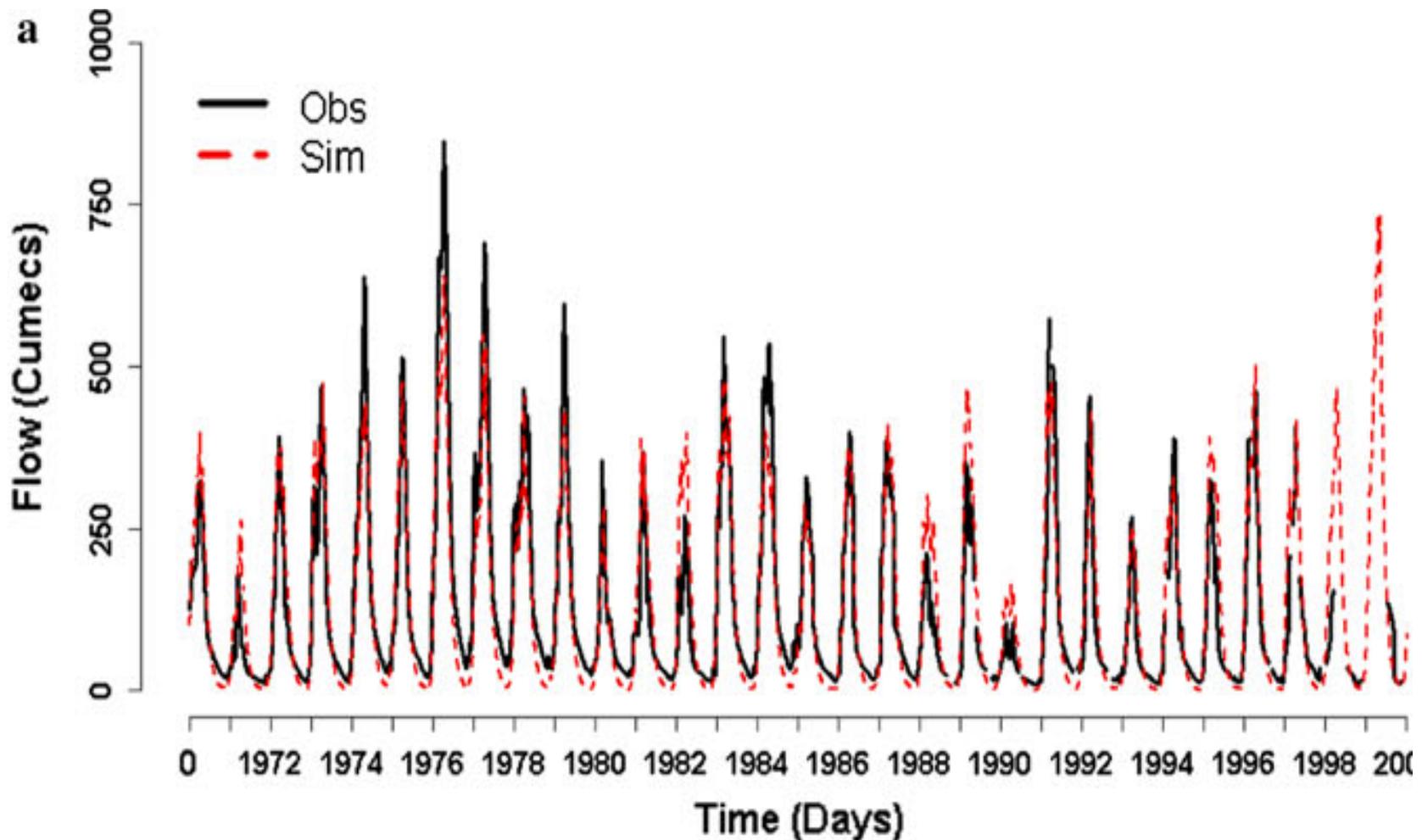
# Parameter determination

- **Parameter estimation:** Set initial range and adjust parameters manually or automatically

# Calibration: Checking Goodness of Fit

- Visual comparison between simulated and observed data – look for trends in errors
  - A learned art, subjective
  - Use appropriate graph
- Statistical and regression based performance measures
  - Consider mean daily discharge as calibration target
  - $Q$  = observed
  - $S$  = simulated

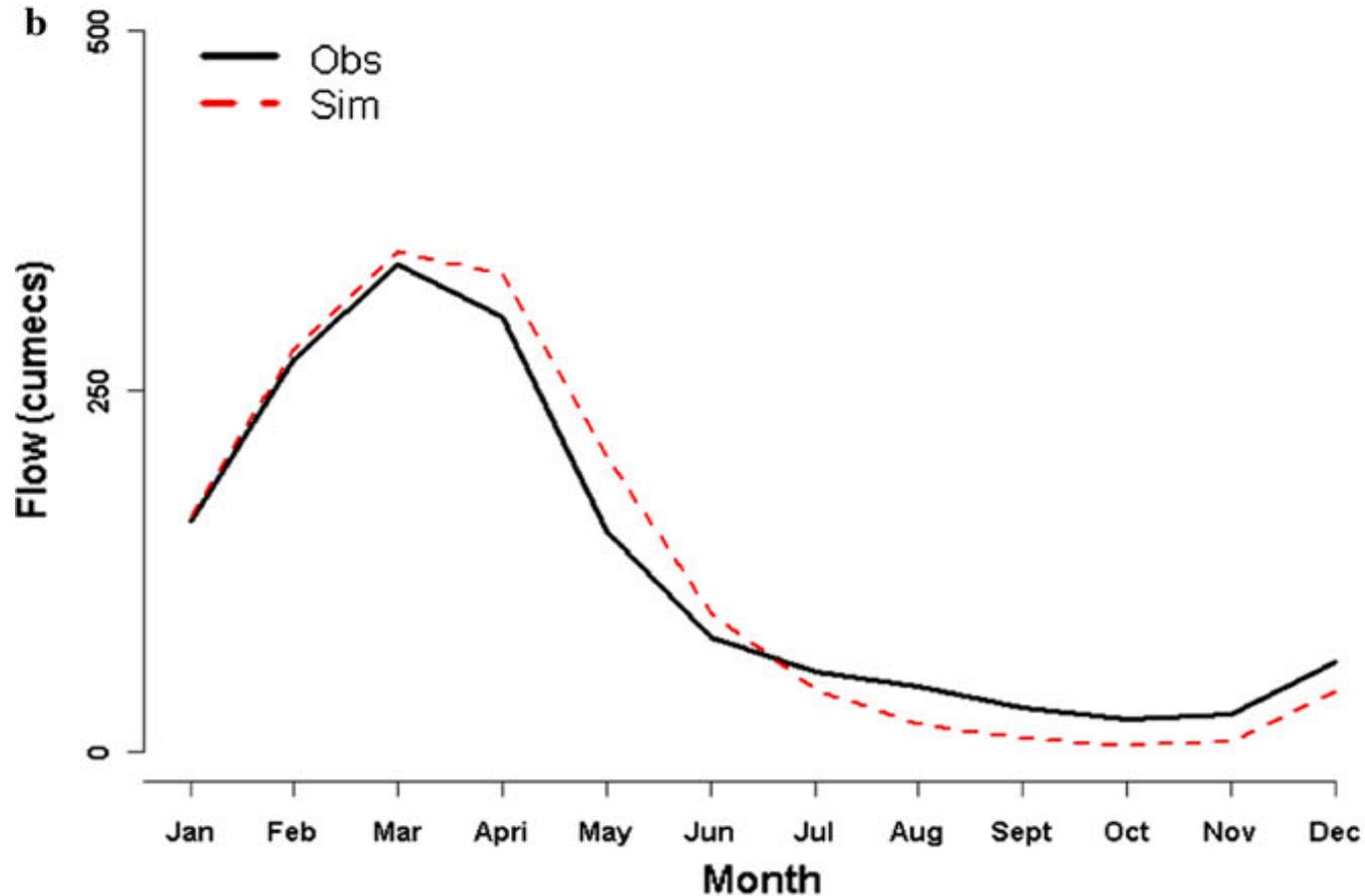
# Calibration and Validation



**Split Sample Test for the WASMOD-D in the Upper Kafue River Basin:  
Calibration 1971–1986) and validation (1987–2001)**

Source: Ngongondo et al. 2013, Stoch Environ Res Risk Assess

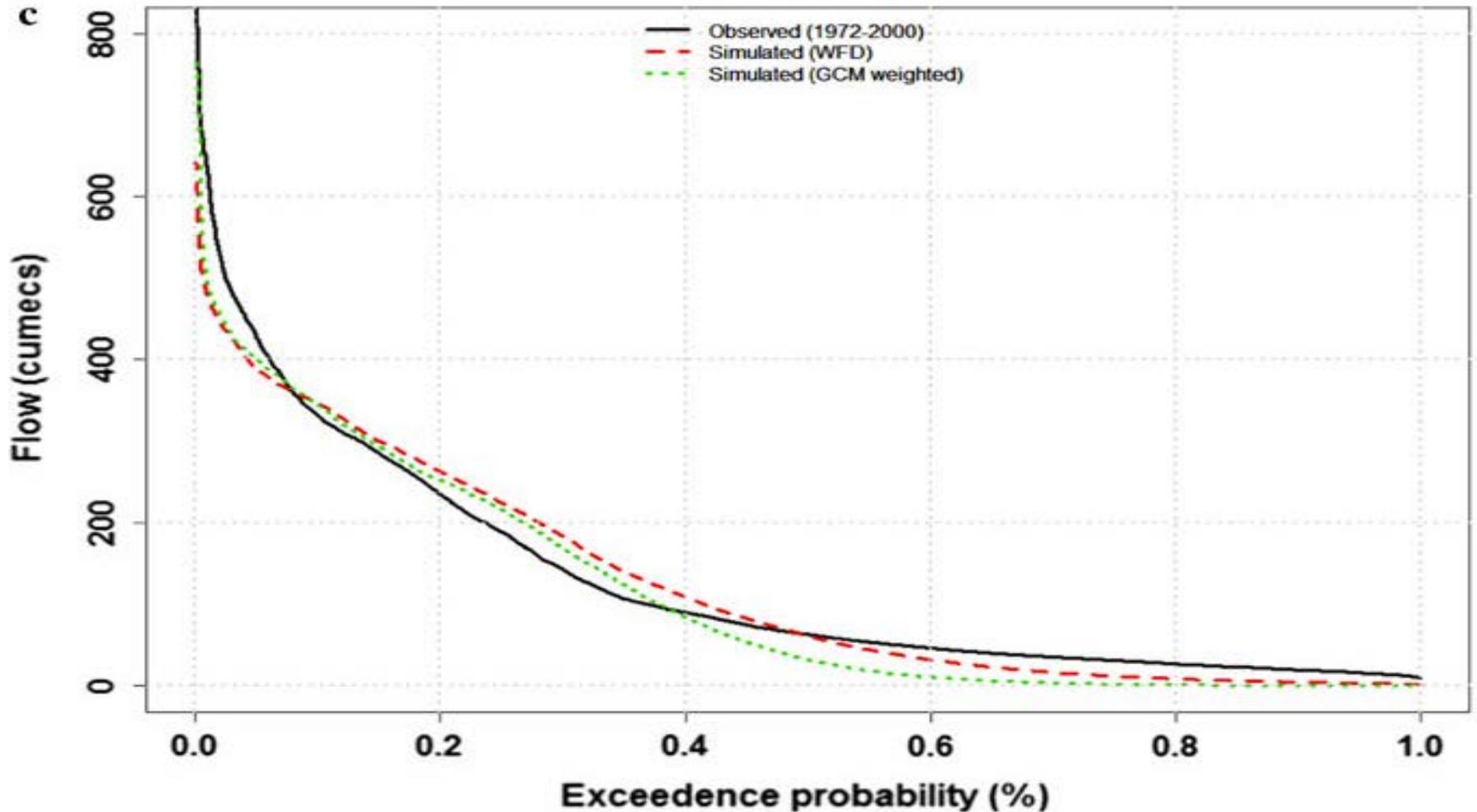
# Calibration and Validation



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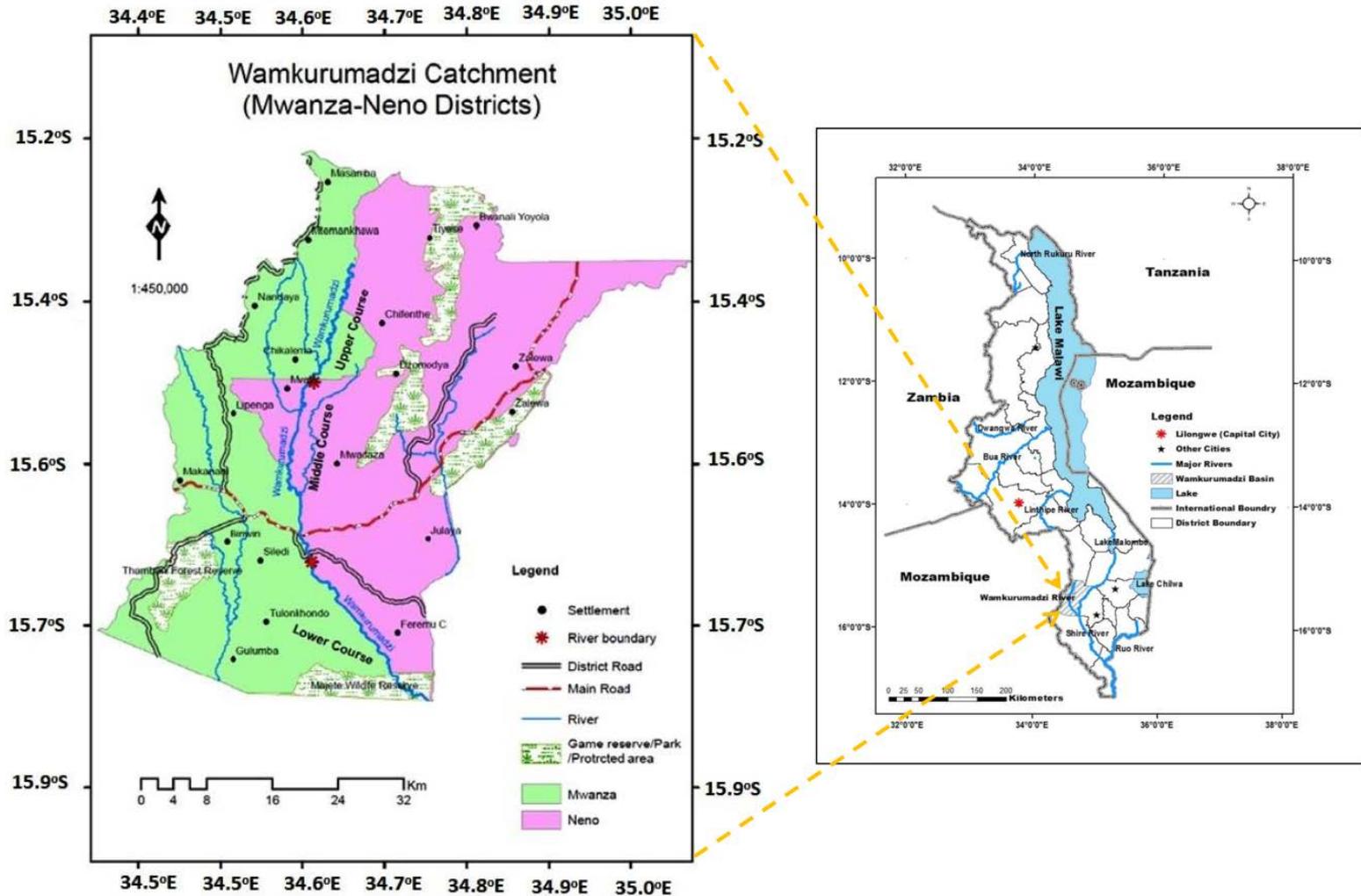
# Calibration and Validation



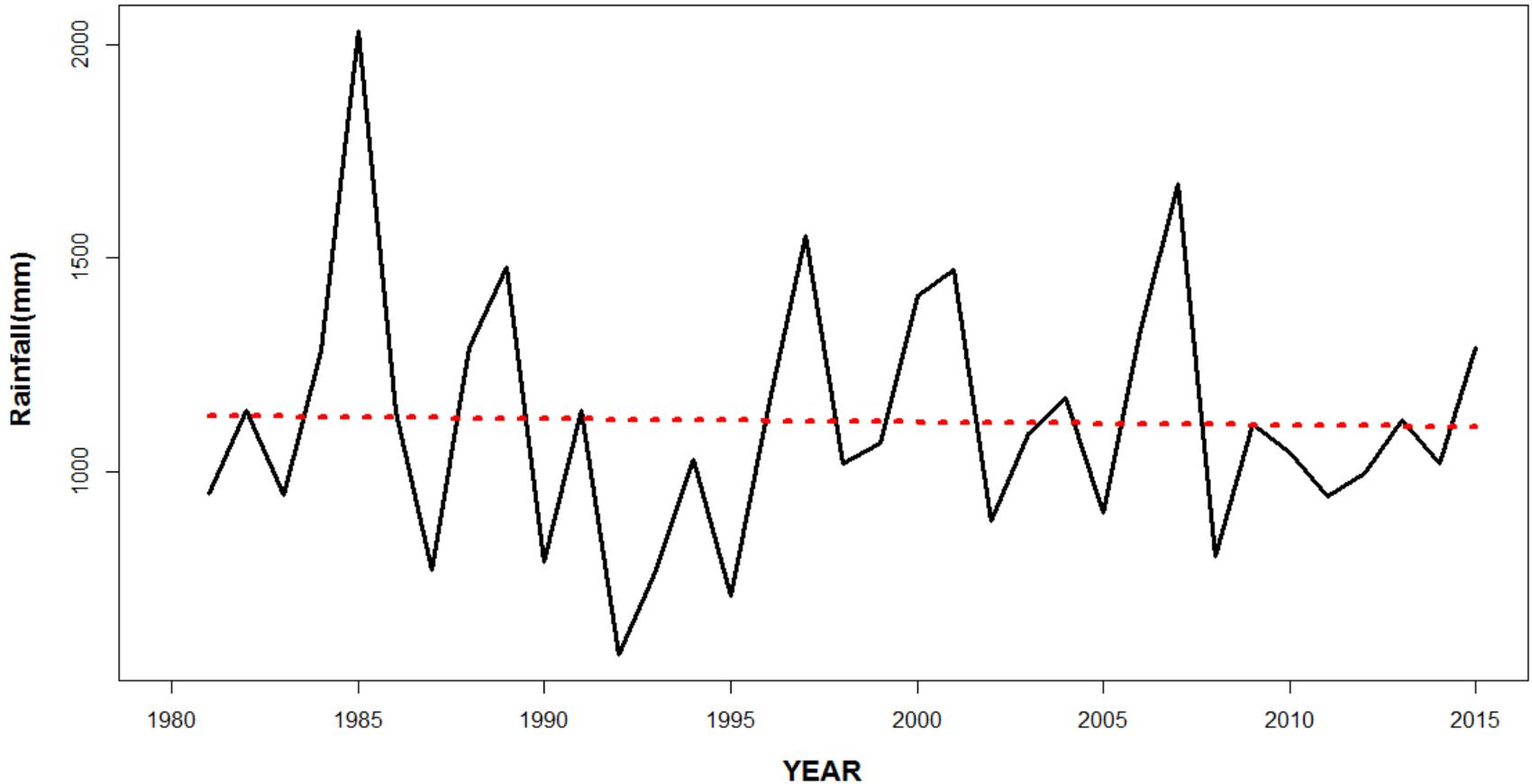
**DC for observed, WFD simulated and GCM weighted discharge for the upper Kafue River at Machiya Ferry (1972–2000)**

Source: Ngongondo et al. 2013, Stoch Environ Res Risk Assess

# Calibration and Validation

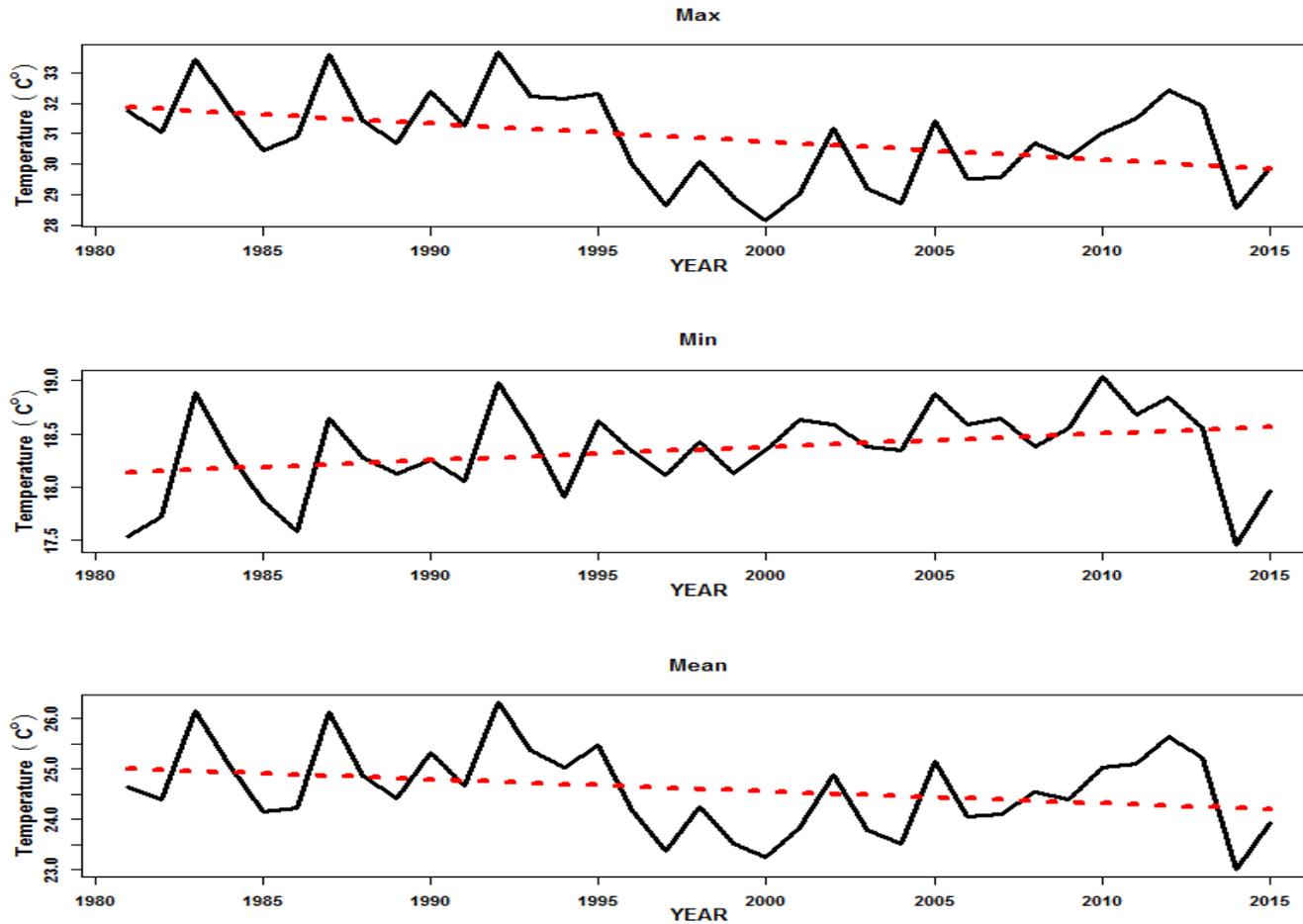


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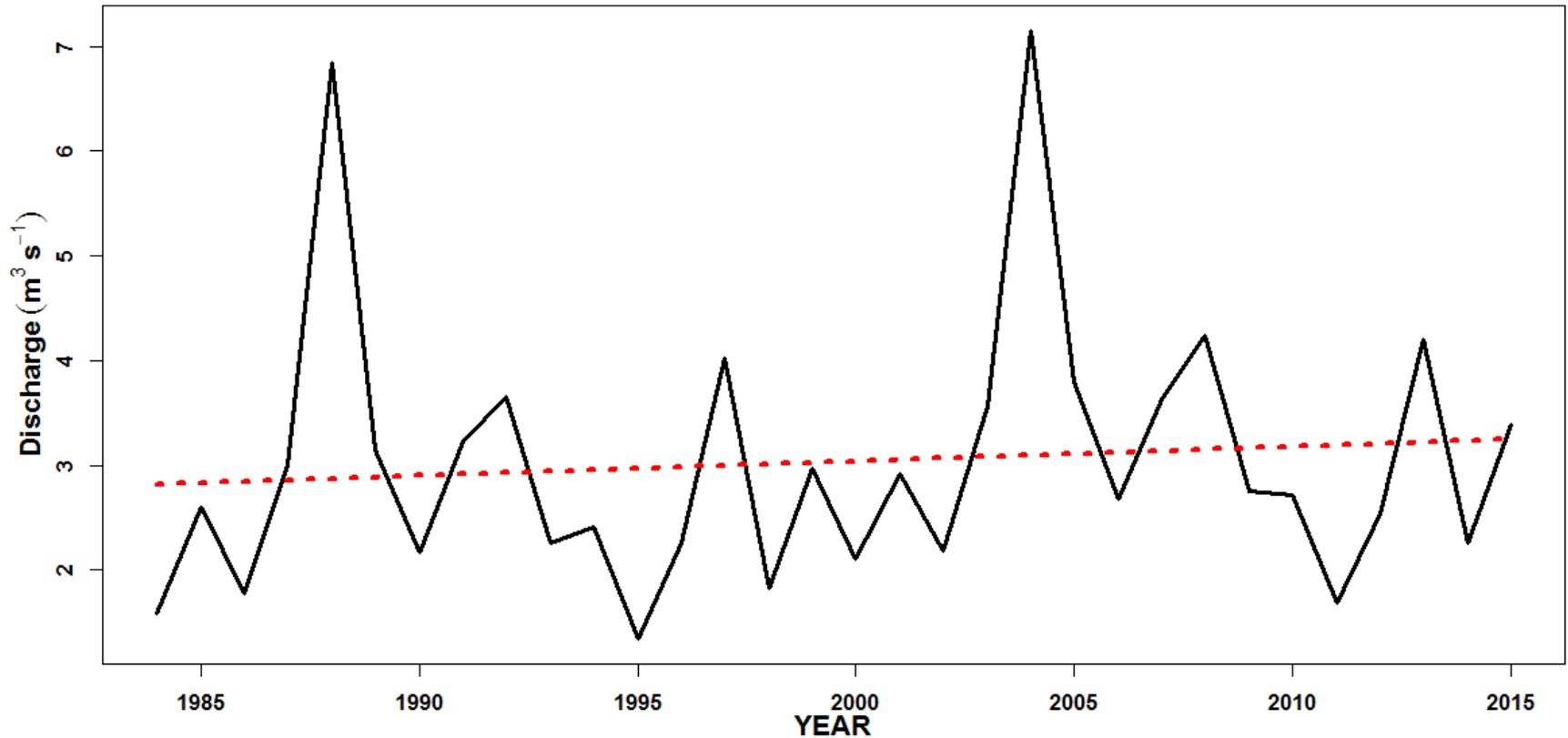


Nkhoma et al. (2020), Water and Climate Change

# Wamkurumadzi

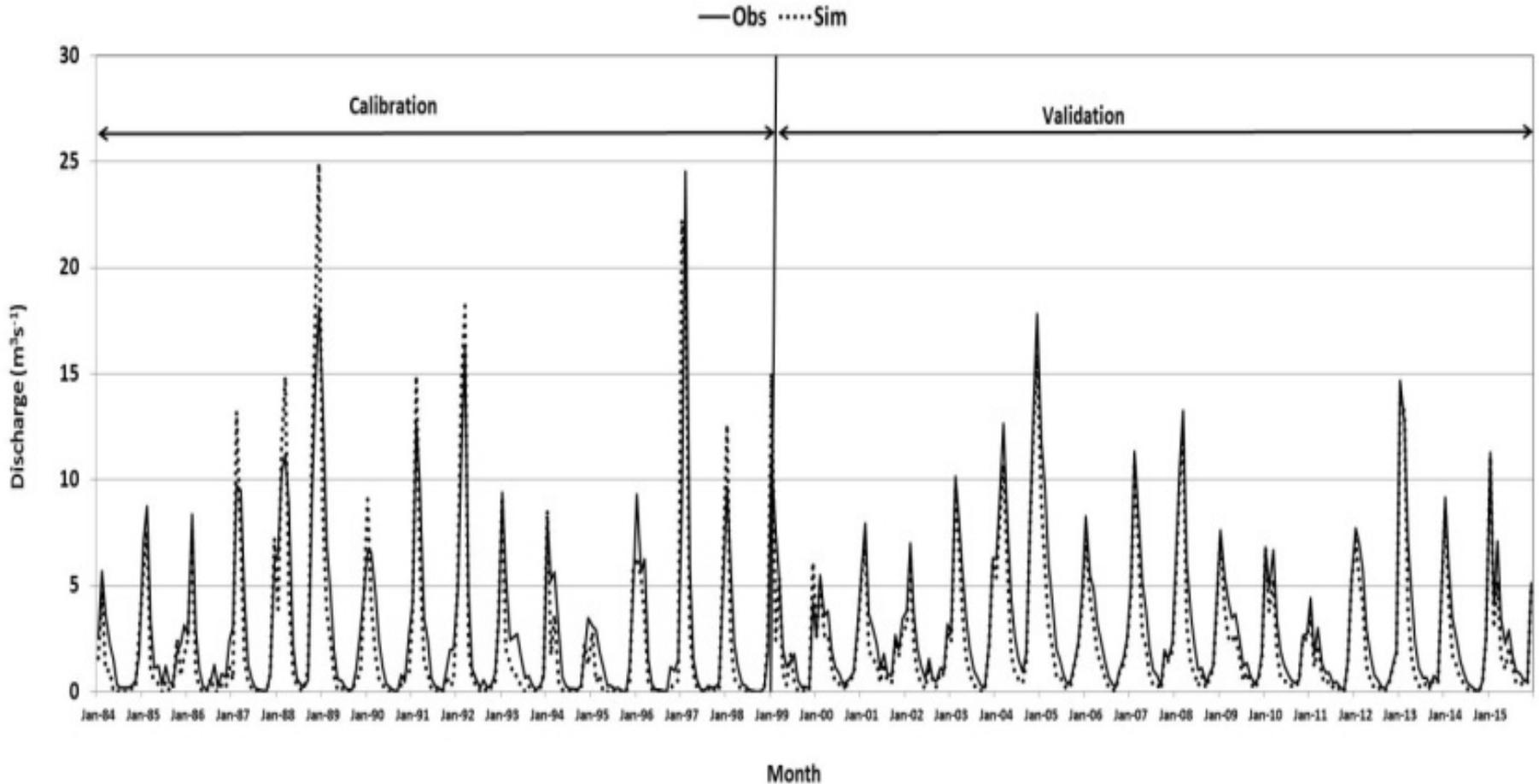


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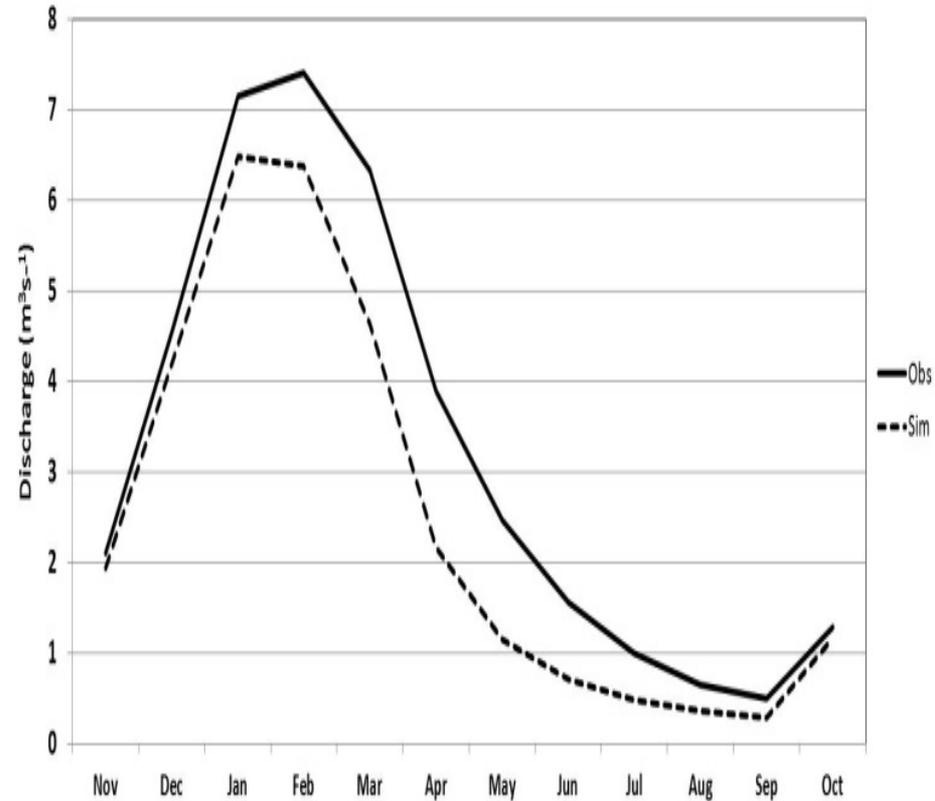
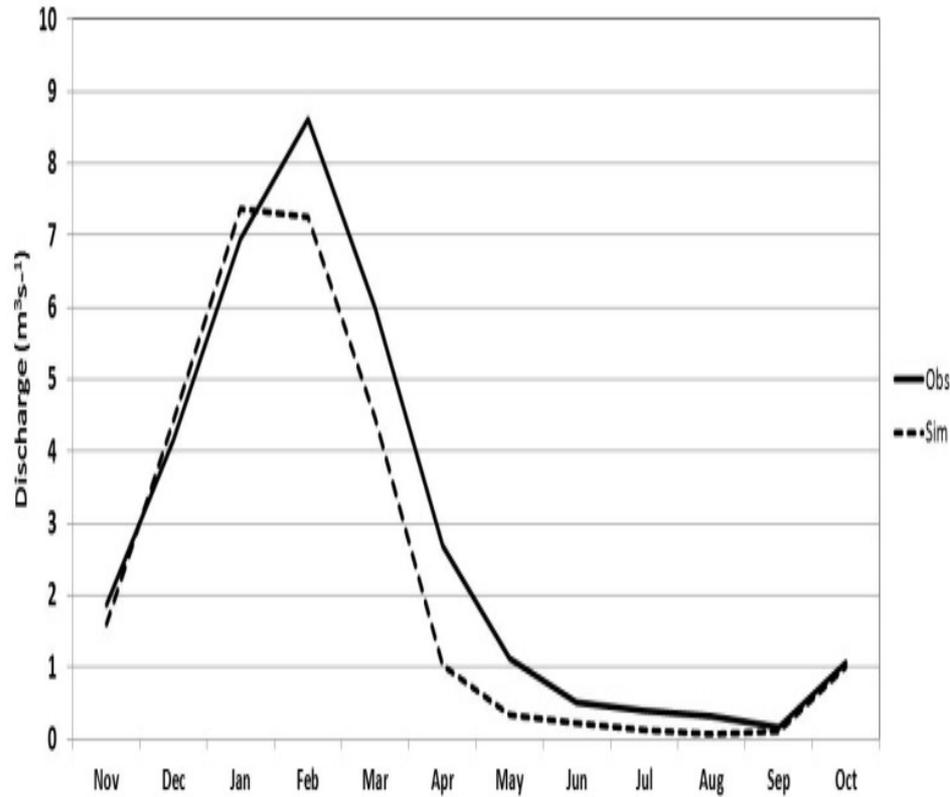


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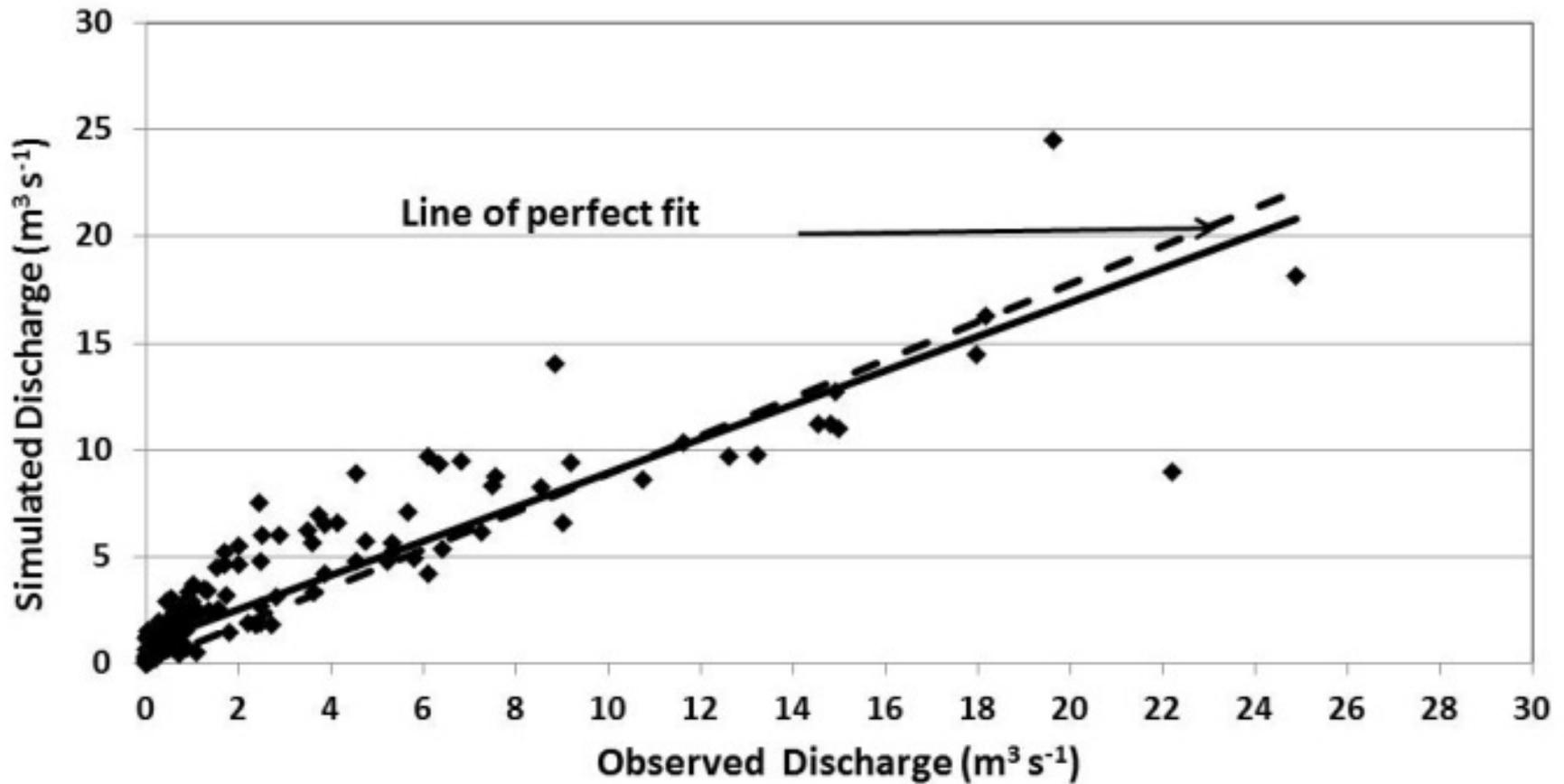
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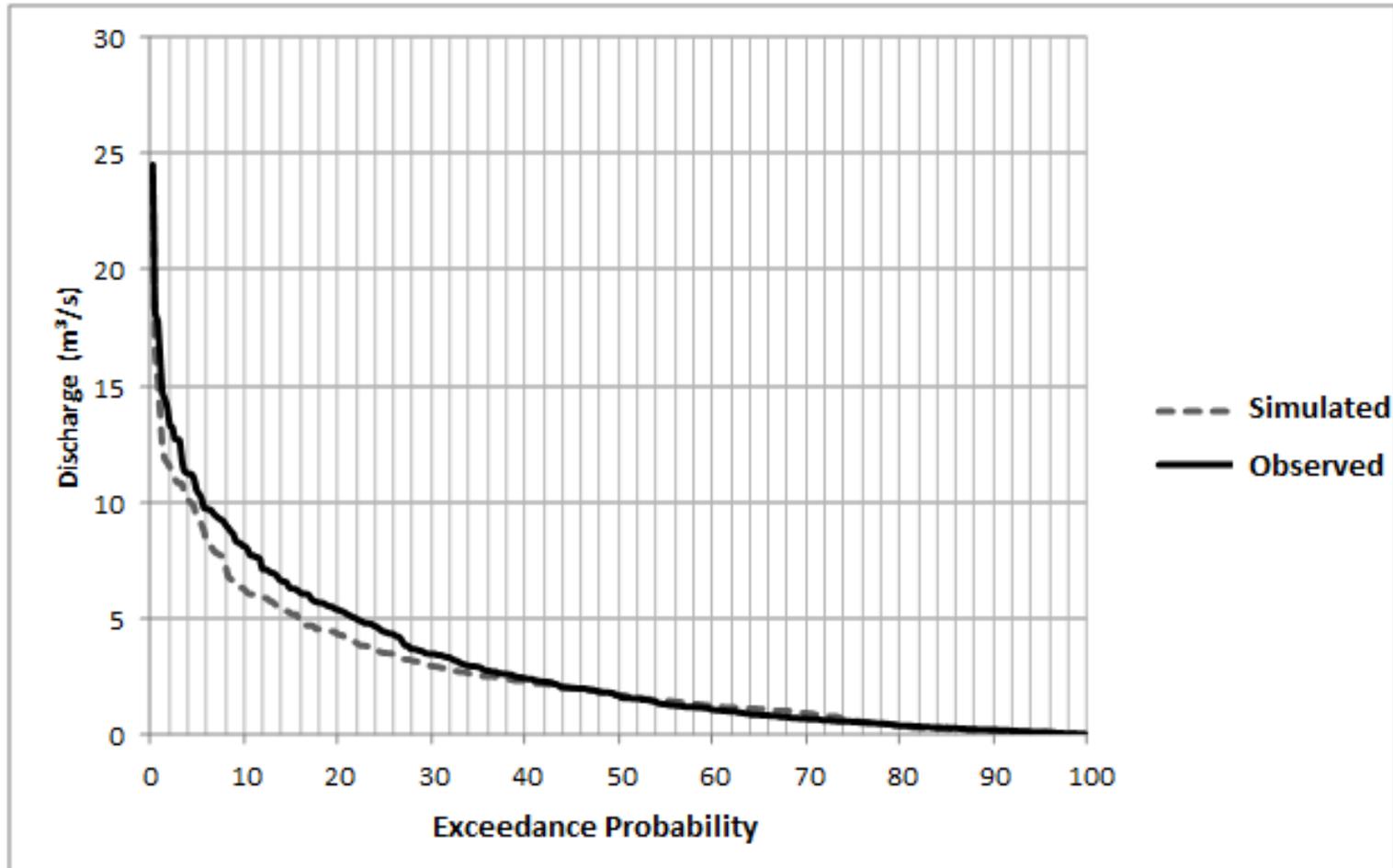
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# Wakurumadzi



# Means and Bias

$$\bar{S} = \frac{\sum_{i=1}^N S_i}{N} \quad \bar{Q} = \frac{\sum_{i=1}^N Q_i}{N}$$

$$\text{Percent Bias} = \frac{\sum_{i=1}^N S_i - Q_i}{\sum_{i=1}^N Q_i} (100)$$

- Common calibration strategy: fix bias first, revisit periodically, goal of no bias
- PBIAS  $\pm 25$  %

- Maximum Error:

$$ME = \max(S_i - Q_i) \text{ for } i = 1 \text{ to } N$$

- Percent Average Absolute Error

$$PAAE = \left\{ \frac{\frac{1}{N} \sum_{i=1}^N |S_i - Q_i|}{\bar{Q}} \right\} (100)$$

# Sum of Squares of Errors

- Most common basis for statistical goodness of fit
  - e.g., least squares regression, seek to minimize

$$\sum_{i=1}^N (S_i - Q_i)^2$$

# Root Mean Squared Error

$$RMSE = \left[ \frac{\sum_{i=1}^N (S_i - Q_i)^2}{N} \right]^{1/2}$$

- Size of error usually related to size of events or values, thus *RMSE* typically smaller for dry periods, small watersheds (for example)

# Percent RMSE

- Normalize *RMSE* by mean observed

$$PRMSE = \frac{RMSE}{\bar{Q}} (100)$$

- Because the magnitude of *RMSE* varies with magnitude of values, by minimizing *RMSE* only, which part of hydrographs are primarily best fit in calibration?

# RSR

- Ratio of the Root Mean Square Error to the standard deviation of measured data

$$RSR = \frac{RMSE}{STDEV_{Obs}}$$

$$RSR \leq 0.70$$

# Nash-Sutcliffe

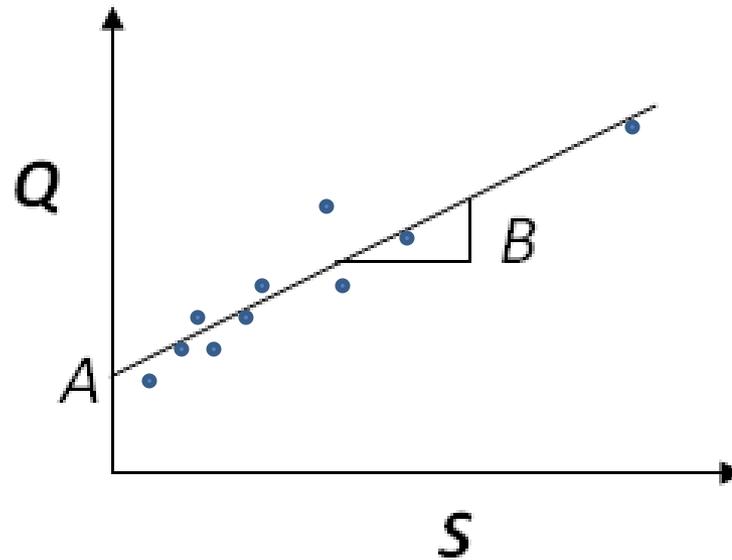
- Very popular method of evaluating calibration

$$R_{NS}^2 = 1 - \frac{\sum_{i=1}^N (S_i - Q_i)^2}{\sum_{i=1}^N (Q_i - \bar{Q})^2}$$

$$R_{NS}^2 \geq 0.5$$

- **Reading:** McCuen, R. H., Evaluation of the Nash—Sutcliffe efficiency index, *Journal of Hydrologic Engineering*, 11(6), 597-602, 2006 (note: author uses different variables)

# Line of Best Fit



$$Q = BS + A$$

*Analyze as in regression: hypothesis testing on  $A$  and  $B$ , residual analysis, correlation coefficient...*

# Recommended Measures

- Moriasi et al. (2007):

Nash–Sutcliffe (NS) coefficient (Nash and Sutcliffe 1970), percent bias error (PBIAS) and ratio of the root mean square error to the standard deviation of measured data (RSR)

# Statistical Indicators

Calibration									Validation										
Period	Mean discharge (m <sup>3</sup> s <sup>-1</sup> )		NS	PBIAS	RSR	Days	R <sup>2</sup>	r		Period	Mean discharge (m <sup>3</sup> s <sup>-1</sup> )		NS	PBIAS	RSR	Days	R <sup>2</sup>	r	
	Obs	Sim									Obs	Sim							
1971–1986	156.4	158	0.83	1.0	0.38	0.96	0.86	0.93		1987–2001	102.04	106.40	0.82	-6.9	0.43	0.95	0.82	0.91	
1987–2001	102.04	110.6	0.82	-2.8	0.43	0.95	0.82	0.90		1971–1986	156.4	154.8	0.83	-2.2	0.41	0.95	0.83	0.91	

**Model performance by simple split-sample test in the upper Kafue River basin during 1971–1986 and 1987–2001**

Source: Ngongondo et al. 2013, Stoch Environ Res Risk Assess

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	Obs	Sim									Obs	Sim							
1971–1980	170.8	165.5	0.84	-3.1	0.40	0.95	0.84	0.92		1981–1990	127.5	120.3	0.82	-3.9	0.42	0.95	0.82	0.91	
1981–1990	127.5	114.8	0.81	-8.2	0.43	0.95	0.83	0.91		1971–1980	170.8	168.2	0.84	-1.6	0.40	0.96	0.84	0.92	

**Model performance by differential split-sample during test wet (1971–1980) and dry years (1981–1990) for the upper Kafue River basin**

Source: Ngongondo et al. 2013, Stoch Environ Res Risk Assess

# Equifinality

- Multiple combinations of parameters can lead to similar results
- Issue with both multi-parameter lumped models (e.g., SAC-SMA) and spatially distributed models (e.g., CASC-2D)
- **Reading:** Ebel, B. A. and K. Loague, Physics-based hydrologic-response simulation: Seeing through the fog of equifinality, *Hydrological Processes*, 20(13), 2887–2900, 2006

End Of Lecture 3